

Reg.No. \_\_\_\_\_

**Karunya UNIVERSITY**

(Karunya Institute of Technology &amp; Sciences)

(Declared as Deemed-to-be University under Sec.3 of the UGC Act, 1956)

**End Semester Examination – Nov/Dec – 2016**

**Code : 14MA2012**  
**Sub. Name : Numerical Methods**

**Semester : 2016-17 ODD**  
**Duration : 3hrs**  
**Max. marks : 100**

Q. No.	Questions				Course outcome	Marks
PART-A (40X1=40 MULTIPLE CHOICE QUESTIONS)						
1.	The approximating curve is_____.				CO1	
	a. Empirical equation	b. Linear law	c. $y = x^2 y - 2$	d. $x_1 + y_1 = 0$		(1)
2.	In $y = ax + b$ , $a$ is called as_____				CO1	
	a. Intercept	b. Slope	c. Origin	d. Point of intersection		(1)
3.	The pattern $y = ax^n$ is reducible to				CO1	
	a. $Y = A + nX$	b. $Y = AX$	c. $y_2 - y_1 = 0$	d. $x_2 - x_1 = 0$		(1)
4.	The method of fitting curve is _____				CO1	
	a. Least squares	b. Unique	c. Isognal method	d. Exponential method		(1)
5.	Slope of the equation $3y = 5x - 6$				CO1	
	a. $\frac{5}{3}$	b. $\frac{5}{6}$	c. 5	d. 6		(1)
6.	The principle of least squares is _____.				CO1	
	a. E is minimum	b. E is maximum	c. $E > a$	d. $E < b$		(1)
7.	$n \sum y = a \sum x + nb$ , n is _____				CO1	
	a zero	b. one	c. Number of observations	d. None of the above		(1)
8.	The linear form of $y = ax^b$ is_____				CO1	
	a. $Y = A + bX$	b. $Y = A - bX$	c. $y = ax + b$	d. $y = ax - b$		(1)
9.	For some observations the normal equations are $55a + 15b + 5c = 200$ , $225a + 55b + 15c = 832$ , $979a + 225b + 55c = 3672$				CO1	
	a. -5.7143, -11.0858, 10.4001	b. 5.7143, 11.0858, 10.4001	c. 5.7143, -11.0858, -10.4001	d. 0, 5.7134, 11, -10.4001		(1)

10.	If $\log_{10} a = 2.5010$ , the value of a is_____.				CO1	
	a. 316.95668	b.200	c.343	d. 0.5962		(1)
11.	If f(a) and f(b) are of _____ , a root of $f(x)=0$ lies between a and b.				CO1	
	a. Opposite signs	b. Same signs	c.Zero	d. One		(1)
12.	For $f(x) = 2x^3 - 3x - 6 = 0$ , find the interval a and b where at least one real root lies				CO1	
	a. 2 and 3	b. 0 and 1	c. 1 and 2	d. 2 and 3		(1)
13.	Formula of Newton Raphson Method_____.				CO1	
	a. $\alpha_{r+1} = \alpha_r - \frac{f(\alpha_r)}{f'(\alpha_r)}$	b. $\alpha_{r+1} = \alpha_{r-1} - \frac{f(\alpha_{r-1})}{f'(\alpha_{r-1})}$	c. $\alpha_r = \frac{f(\alpha_r)}{f'(\alpha_r)}$	d. $\alpha_{r+1} = \alpha_r$		(1)
14.	For a system of 3 simultaneous linear algebraic equations, $(A, B) = \begin{pmatrix} 2 & 3 & -1 & 5 \\ 0 & -2 & -1 & -7 \\ 0 & 0 & 6 & 18 \end{pmatrix}$ , find the value of $x, y, z$ .				CO1	
	a. 2, -1, 3	b. 1, -1, -1	c. 0, 1, 2	d. 1, 2, 3		(1)
15.	The system linear algebraic equations are equivalent to the form _____.				CO1	
	a. $AX = B$	b. $A = B$	c. $AXB = 0$	d. $A'X = B$		(1)
16.	To find the interpolation value nearby central value using the method_____.				CO2	
	a. Gauss's Interpolation formula	b. Newton's Interpolation formula	c. Factorial Polynomial	d. All the above		(1)
17.	In Gauss's backward interpolation formula the value of u is _____.				CO2	
	a. $\frac{x+x_0}{h}$	b. $\frac{x-x_0}{h}$	c. $\frac{x-x_n}{h}$	d. $x-x_n$		(1)
18.	Gauss's Forward formula involves _____ differences below the central line and _____ differences on the line.				CO2	
	a. Odd, odd	b. even, even	c. odd, even	d. even, odd		(1)
19.	Gauss's backward formula can be used when the value of u lies between _____				CO2	
	a. -1 and 1	b. -1 and 0	c. 1 and 2	d. 0 and 1		(1)
20.	Find the polynomial passing through the points (0,0), (1,1), (2,20)				CO2	
	a. $y = 9x^2 + 8x$	b. $y = x^2 + 8x$	c. $y = 9x^2 - 18x$	d. $y = 9x^2 - 8x$		(1)
21.	Let $y=f(x)$ . The process of finding x when y is given _____				CO2	
	a. Inverse Lagrange's formula	b. Gauss's Interpolation formula	c. Newton's Interpolation formula	d. Exponential method		(1)

22.	The error in the trapezoidal rule of the order_____.				CO3	
	a. $h$	b. $h+1$	c. $h-1$	d. $h^2$		(1)
23.	In Newton Cote's quadrature formula, setting n=1 we get _____				CO3	
	a. Newton's forward formula	b. Gauss's formula	c. Trapezoidal rule	d. Simpson's rule		(1)
24.	The truncation error in Trapezoidal rule is _____				CO3	
	a. $ E  < \frac{(b-a)h^2}{12}$	b. $ E  < \frac{(b-a)h^2}{12} M$	c. $ E  > \frac{(b-a)h^2}{12} M$	d. $ E  < \frac{(b-a)^2}{12} M$		(1)
25.	Simpson's three-eighth rule is applicable when the number of intervals n is _____.				CO3	
	a. odd	b. even	c. Multiple of 3	d. Multiple of 2		(1)
26.	The error in the Simpson's one-third rule of the order_____.				CO3	
	a. $h$	b. $h+1$	c. $h-1$	d. $h^4$		(1)
27.	Simpson's one-third rule is applicable when the number of intervals n is _____.				CO3	
	a. 1	b. 0	c. odd	d. enen		(1)
28.	In Newton Cote's quadrature formula, setting n=2 we get _____				CO3	
	a. Simpson's one-third rule	b. Gauss's formula	c. Trapezoidal rule	d. Newton's formula		(1)
29.	In trapezoidal rule the interpolating polynomial is _____.				CO3	
	a. Linear	b. Polynomial of degree 2	c. Polynomial of degree 3	d. Polynomial of degree n		(1)
30.	The truncation error in Simpson's one third rule is _____				CO3	
	a. $ E  < \frac{(b-a)h^4}{180} M$	b. $ E  < \frac{(b-a)h^2}{12} M$	c. $ E  > \frac{(b-a)h^2}{12} M$	d. $ E  < \frac{(b-a)^2}{12} M$		(1)
31.	In Newton Cote's quadrature formula, setting n=3 we get _____				CO3	
	a. Simpson's one-third rule	b. Gauss's formula	c. Trapezoidal rule	d. Simpson's three-eighths rule		(1)
32.	A factorial polynomial $x^{(2)} =$ _____				CO2	
	a. $x-h$	b. $x(x-h)$	c. $x(x-h)(x-h)^2$	d. $x(x-h)(x-2h)$		(1)
33.	$\Delta^n y_i =$				CO2	
	a. $\Delta^{n-1} y_{i+1} - \Delta^{n-1} y_i$	b. $\Delta^{n-1} y_{i+1}$	c. $\Delta^{n-1} y_i$	d. $\Delta^{n-1} y_{i+1} + \Delta^{n-1} y_i$		(1)
34.	The sum of the squares of the residuals of straight line fit is _____				CO1	
	a. $E = \sum y^2 - a \sum xy - b \sum y$	b. $E = \sum y^2 - a \sum xy$	c. $E = ax^2 + bx + c$	d. $E = ax^2 y + bx$		(1)

35.	In Newton forward interpolation method $u =$				CO2	
	a. $\frac{x}{h}$	b. $\frac{x - x_n}{h}$	c. $\frac{x_n}{h}$	d. $\frac{x - x_0}{h}$		(1)
36.	For solving a system of 3 equations, the initial values in Gauss Seidel Method				CO1	
	a. $x = 1, y = 1, z = 1$	b. $x = 0, y = 1, z = 1$	c. $y = 0, z = 0$	d. $x = 0, y = 0, z = 0$		(1)
37.	Relation between $E$ and $\Delta$ is _____				CO2	
	a. $E = \Delta$	b. $E = \Delta + 1$	c. $E = \Delta - 1$	d. $E = 1$		(1)
38.	Error in the Taylor series method is _____				CO3	
	a. $\frac{h^n}{n!} f^n(\theta)$	b. $\frac{h^n}{n!} f^{n+1}(\theta)$	c. $\frac{h^{n+1}}{n!} f^{n+1}(\theta)$	d. $\frac{h^n}{(n+1)!} f^{n+1}(\theta)$		(1)
39.	In Runge Kutta method the solution $y(x+h) =$ _____				CO3	
	a. $y(x) + \Delta y$	b. $y(x) - \Delta y$	c. $y(x) + h\Delta y$	d. $y(x) - h\Delta y$		(1)
40.	In Runge Kutta third order $\Delta y =$ _____				CO3	
	a. $\frac{1}{6}(k_1 + 4k_2 - k_3)$	b. $\frac{1}{6}(k_1 - 4k_2 + k_3)$	c. $\frac{1}{6}(k_1 + 4k_2 + k_3)$	d. $\frac{1}{6}(2k_1 + 4k_2 - k_3)$		(1)

**PART B(8 X 5 = 40 MARKS) (ANSWER ANY EIGHT)**

41.	Fit a curve of the form $y = ax^b$ to the data	CO1	(5)														
	<table><tr><td>X:</td><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td></tr><tr><td>Y:</td><td>1200</td><td>900</td><td>600</td><td>200</td><td>110</td><td>50</td></tr></table>	X:	1	2	3	4	5	6	Y:	1200	900	600	200	110	50		
X:	1	2	3	4	5	6											
Y:	1200	900	600	200	110	50											
42.	Find the positive root of $f(x) = 2x^3 - 3x - 6 = 0$ by Newton-Raphson method correct to four decimal places.	CO1	(5)														
43.	Solve the following system of equations by Gauss-seidel method $5x - 2y + z = -4, x + 6y - 2z = -1, 3x + y + 5z = 13$	CO1	(5)														
44.	From the following data find the value of y at x=1976 using Newton's backward interpolation formula:	CO2	(5)														
	<table><tr><td>X:</td><td>1941</td><td>1951</td><td>1961</td><td>1971</td><td>1981</td><td>1991</td></tr><tr><td>Y:</td><td>20</td><td>24</td><td>29</td><td>36</td><td>46</td><td>51</td></tr></table>	X:	1941	1951	1961	1971	1981	1991	Y:	20	24	29	36	46	51		
X:	1941	1951	1961	1971	1981	1991											
Y:	20	24	29	36	46	51											
45.	Find the seventh term of the sequence 2,9,28,65,126,217	CO2	(5)														
46.	Apply Gauss's forward central difference formula and estimate f(32) from the following table:	CO3	(5)														
	<table><tr><td>X:</td><td>25</td><td>30</td><td>35</td><td>40</td></tr><tr><td>Y:</td><td>0.2707</td><td>0.3027</td><td>0.3386</td><td>0.3794</td></tr></table>	X:	25	30	35	40	Y:	0.2707	0.3027	0.3386	0.3794						
X:	25	30	35	40													
Y:	0.2707	0.3027	0.3386	0.3794													
47.	Using Lagrange's formula of interpolation find y(10) from the following data:	CO3	(5)														
	<table><tr><td>X:</td><td>5</td><td>6</td><td>9</td><td>11</td></tr><tr><td>Y:</td><td>12</td><td>13</td><td>14</td><td>16</td></tr></table>	X:	5	6	9	11	Y:	12	13	14	16						
X:	5	6	9	11													
Y:	12	13	14	16													
48.	Using Taylor's method, compute y(1.1) and correct to three decimal places given	CO3	(5)														

	$\frac{dy}{dx} = x + y$ and $y(0)=1$ .		
49.	Solve the equation $\frac{dy}{dx} = 1 - y$ , given $y(0)=0$ using Modified Euler's method and  Find $y(0.1)$ .	CO3	(5)
50.	Obtain the values of $y$ at $x=0.1$ , using Runge-kutta method of fourth order for the differential equation $\frac{dy}{dx} = -y$ , given $y(0)=1$	CO3	(5)
<b>PART C( 2 X 10 = 20 MARKS) (ANSWER ANY TWO)</b>			
51.	Fit a straight line and parabola to the following data and find out which one is most appropriate.  <div style="display: flex; justify-content: space-around; margin-top: 10px;"> <div style="text-align: center;">X: 1      2      3      4      5</div> <div style="text-align: center;">Y: 10    12    8      10    14</div> </div>	CO1	(10)
52.	Solve the system of equations by Gauss-Jordan method  $x + 2y + z = 3, 2x + 3y + 3z = 10, 3x - y + 2z = 13$	CO1	(10)
53.	Evaluate $\int_{-3}^3 x^4 dx$ using (i) Trapezoidal rule, (ii) Simpson's one- third, (iii) Simpson's three-eighth rule.	CO3	(10)

ALL THE BEST